# LOW EARTH ORBIT SATELLITE RAIN ATTENUATION ANALYSIS: CASE STUDY OF IRIDIUM 914 SATELLITE

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Abstract- In this paper, low earth orbit satellite rain attenuation analysis is presented. The case study is Iridium 914 satellite and the earth station is at University of Uyo at latitude of 5.028933°, longitude of 7.978991° and magnetic declination of 0° 52' W. The orbital track data with respect to the earth station gave elevation angles in the range of 10° to 74°. The International Telecommunication Union (ITU) powerlaw model which expresses rain attenuation in terms of specific rain attenuation and some frequency and polarization dependents parameters was used. The results show that the specific rain attenuation is not affected by the elevation angle but it is affected by the signal polarization. Accordingly, the specific rain attenuation for the horizontal polarized signal is higher for all the elevation angles than that of the vertical polarized signal. Also, the results show that the rain attenuation is inversely proportional to elevation angle. Hence, the rain attenuation is high for low elevation angle but low for high elevation angle. Furthermore, the rain attenuation for the horizontal polarized signal is higher for all the elevation angles than that of the vertical polarized signal. In addition, the rain attenuation is inversely proportional to rain fall exceeded percentages, P. Hence, the rain attenuation is high for low P but low for high P. In all, in this paper, the ideas presented is very relevant to satellite link designers in the selection of equipment and parameter values for different rain zones and desired network availability.

Keywords— Low Earth Orbit Satellite, Rain Attenuation, Network Availability, Specific Rain Attenuation, Iridium 914 Satellite, Magnetic Declination, Power-Law Model, Polarized Signal

#### 1. Introduction

Today, satellite technologies have become widely adopted in diverse applications that include remote sensing, weather forecasting, reconnaissance, navigation, and various forms of communications [1,2,3,4,5,6,7,8,9,10]. The specific application determines the type of satellite to be deployed. In this paper, the Iridium satellite is considered. Basically, the Iridium satellite is a constellation of about 66 satellites that are used to provide global coverage for voice and data communication among handheld mobile devices [11,12,13,14,15,16,171,18,19,20]. Such communication system utilizes wireless signal in the high frequency microwave bands which are significantly affected by rain attenuation [21,22,23,24,25,26,27,28]. As such, the quality of service of such satellite link can be effected by rainfall in the regions where the earth stations are located.

Again, Iridium satellite is a Low Earth Orbit (LEO) satellite which means that its position relative to a given earth station changes with time [29,30,31,32,33,34]. The changing position entails changes in the elevation angle which also affect other parameters of the rain attenuation that can be suffered by the wireless signal used in the satellite link. Accordingly, in this paper, the analysis of the rain attenuation of the Iridium satellite-earth station link is conducted. The analysis used satellite tracking dataset to determine the position and the corresponding elevation angles of the Iridium satellite over its repeat cycle. The analysis considered the variation of the specific rain attenuation, the effective rain path length and the rain attenuation with elevation angles of the Iridium satellite link relative to a given earth station location. Matlab software was used to carry out the computations.

# 2. Methodology

The model used is the International Telecommunication Union (ITU) **power-law** rain attenuation computation model which expresses rain attenuation in terms of specific rain attenuation and some frequency and polarization dependents parameters, along with effective rain path length. However, the effective rain path length is determined from the rain slant path length,  $L_s$  and  $L_g$  which is the horizontal projection distance covered by  $L_s$ , as shown in Figure 1.



Figure 1 The diagram for modelling the rain slant path length,  $L_s$ 

The rain attenuation for horizontally or vertically polarized signal is considered. Let the specific rain attenuation for vertically polarized signal be denoted as  $\gamma_v$ , then ;

$$\gamma_{\nu} = k_{\nu} \left( R_{\nu} \right)^{\alpha_{\nu}} \tag{1}$$

Let the specific rain attenuation for horizontal polarized signal be denoted as  $\gamma_h$ , then ;

$$\gamma_h = k_h \left( R_p \right)^{\alpha_h} \tag{2}$$

Where the values of the parameters,  $k_{\nu}$ ,  $\alpha_{\nu}$ ,  $k_h$  and  $\alpha_h$  depend on the frequency and the the signal polarization category. The rain slant path length,  $L_s$  is given in terms of rain height (H<sub>r</sub>), the earth station altitude or height (H<sub>e</sub>) and the satellite link elevation angle ( $\theta_e$ ) as follows;

$$L_s = \frac{H_r - H_e}{\sin(\theta_e)} \tag{3}$$

The horizontal projection distance covered by  $L_s$  on the ground is denoted as  $L_g$  where;

$$L_g = (L_s)\cos(\theta_e) \tag{4}$$

The rain path length reduction factor,  $(r_p)$  for different rain fall exceeded percentages, P is computed as follows;

$$r_{p} = \begin{cases} \frac{10}{10 + L_{g}} & for \ p = 0.001\% \\ \frac{90}{90 + 4(L_{g})} & for \ p = 0.01\% \\ \frac{180}{180 + L_{g}} & for \ p = 0.1\% \\ 1 & for \ p = 1\% \end{cases}$$
(5)

Let the effective rain path length be denoted as  $L_e$ , then ;

$$L_{e} = L_{s}(r_{p}) = \left(\frac{H_{r} - H_{e}}{\sin(\theta_{e})}\right)(r_{p})$$
(6)

Let the rain attenuation for horizontally or vertically polarized signal be denoted as  $A_R$ , then;

$$A_{\rm R} = \begin{cases} L_s(r_p)\gamma_v & \text{for vertically polarized signal} \\ L_s(r_p)\gamma_h & \text{for horizontally polarized signal} \end{cases}$$
(7)

 $A_{\rm R} = \begin{cases} L_{\rm e}(r_p) (k_v \ (R_p)^{\alpha_v}) & \text{for vertically polarized signal} \\ L_{\rm e}(r_p) (k_h \ (R_p)^{\alpha_h}) & \text{for horizontally polarized signal} \end{cases} (8)$ 

Let  $A_{R0.01}$  denote rain attenuation computed at p = 0.01 %, where  $A_{R0.01}$  is in dB, then rain attenuation at other values of p can be obtained as follows, ;

$$A_{\rm Rp} = \begin{cases} A_{\rm R0.01} \left( 0.12 p^{-(0.546 + 0.043(Log(p)))} \right) & for \ Lat_{es} \ge 30^{\circ} \\ A_{\rm R0.01} \left( 0.07 p^{-(0.855 + 0.139(Log(p)))} \right) & for \ Lat_{es} < 30^{\circ} \end{cases}$$
(9)

Where  $Lat_{es}$  is the latitude of the earth station.

The case study LEO satellite is IRIDIUM 914 and the summary of key parameters of the satellite are presented in Table 1. The earth station is at University of Uyo, Aka Ibom Nigeria, with latitude of 5.028933°, longitude of 7.978991° and magnetic declination of 0° 52' W. The IRIDIUM 914 10-day live tracking predictions dataset based on earth station observation location coordinates of 5.028933, 7.978991is presented in Table 2 and Figure 2. Based on the dataset in Table 1, the following elevation angles are used :  $10^{\circ}$ ,  $18^{\circ}$ ,  $26^{\circ}$ ,  $41^{\circ}$ ,  $49^{\circ}$ ,  $52^{\circ}$ ,  $60^{\circ}$ ,  $69^{\circ}$  and 74°. Also, the rainfall rates exceeding 0.01% of an average year in Uyo is 124 mm/hr [35]. Also, Iridium operates in frequency of **1** – **2** L-band GHz the

Table 1	The launch detail	and orbital elements	of IRIDIUM 914
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Launch Detail					
Launched	18 June 1997				
Status	Non-operational				
Category	Iridium				
Launch site	Tyuratam Missile and Space Center, Kazakhstan (Also known as Baikonur Cosmodrome)				
Owner	United States				
NORAD ID	24836				
COSPAR ID	1997-030A				
	Current orbital elements				
Inclination	86.391°				
Eccentricity	0.00037				
RA ascending node	6.450 hr				
Argument perihelion	105.492°				
Mean anomaly	254.669°				
Orbital period	100.071 min				
Epoch of osculation	05 May 2021, 22:31				



Figure 2 IRIDIUM 914 live tracking predictions map showing the orbit track (yellow line), the ground foot print of the satellite and the earth station

Table 2 IRIDIUM 914 10-day live tracking predictions dataset	based on earth station observation location coordinates
of 5.02893	33, 7.978991

Start 🕈		Max altit	ude		End 븆		All passes
Date, Local time Az		Local time	Az	El	Local time Az		Mag 🛈
8-May 03:57	N 351°	04:04	W 274°	52°	04:11	S 190°	+9.5
8-May 14:51	SSE 154°	14:58	E 90°	23°	15:04	NNE 24°	+8.5
8-May 16:31	SSW 209°	16:38	W 271°	19°	16:44	NNW 333°	+8.7
9-May 03:18	N 7°	03:26	E 92°	60°	03:33	S 173°	+9.6
9-May 15:52	S 191°	16:00	W 270°	49°	16:07	N 350°	+7.4
10-May 02:41	NNE 23°	02:48	E 89°	23°	02:54	SSE 154°	+9.9
10-May 04:21	NNW 333°	04:28	W 273°	19°	04:34	SW 211°	+9.9
10-May 15:14	S	15:21	E	63°	15:29	Ν	+7.1

Start 🕈		Max altitu	ude		End 븆		All passes	
Date, Local time	Az	Local time Az El		Local time	Az	Mag 0		
	173°		94°			6°		
11-May 03:42	N 350°	03:50	W 271°	48°	03:57	S 192°	+9.8	
11-May 14:37	SSE 156°	14:43	E 88°	24°	14:50	NNE 23°	+8.4	
11-May 16:17	SW 210°	16:23	W 270°	18°	16:30	NNW 331°	+8.8	
12-May 03:04	N 5°	03:11	Е 85°	65°	03:19	S 174°	+9.9	
12-May 15:38	S 192°	15:45	W 272°	45°	15:52	N 349°	+7.5	
13-May 02:27	NNE 22°	02:33	Е 91°	25°	02:40	SSE 156°	-	
13-May 04:07	NNW 331°	04:13	W 272°	17°	04:20	SW 213°	-	
13-May 15:00	S 175°	15:07	E 89°	69°	15:14	N 5°	+7.1	
14-May 03:28	N 348°	03:35	W 269°	44°	03:42	S 193°	-	
14-May 14:22	SSE 157°	14:29	E 90°	26°	14:36	NNE 22°	+8.3	
14-May 16:03	SW 213°	16:09	W 271°	17°	16:15	NW 329°	+8.9	
15-May 02:50	N 4°	02:57	E 90°	71°	03:04	S 176°	-	
15-May 15:24	S 193°	15:31	W 269°	42°	15:38	N 347°	+7.7	
16-May 02:12	NNE 20°	02:19	E 89°	27°	02:26	SSE 157°	-	
16-May 03:53	NW 329°	03:59	W 271°	16°	04:05	SW 214°	-	
16-May 14:46	S 176°	14:53	E 80°	74°	15:00	N 3°	+7.0	
17-May 01:36	NE 41°	01:41	E 88°	10°	01:46	SE 136°	-	
17-May 03:14	N 347°	03:21	W 272°	41°	03:28	S 195°	-	
17-May 14:08	SSE 158°	14:15	E 89°	28°	14:22	NNE 20°	+8.2	

Legend: Not visible Marginal Good Excellent

#### (Source: <u>https://www.n2yo.com/passes/?s=24836</u>)

# 3. Result and Discussion

The cases study IRIDIUM 914 satellite link elevation angles ranging from 10° to 74° were extracted from a 10day live tracking predictions dataset based on earth station observation location coordinates of 5.028933, 7.978991. The elevation angles were then used in the analytical expressions presented in this paper to determine the rain slant path length and hence the effective rain path length, as shown in Table 3. The graph plot of the effective rain path length versus elevation angle is given in Figure 3. The results in Table 3 and Figure 3 show that the effective rain path length is inversely proportional to elevation angle. Hence, the effective rain path length is high for low elevation angle but low for high elevation angle.

The results of the computation for the specific rain attenuation as a function of elevation angle are presented in Table 4 and Figure 4. The results in Table 4 and Figure 4 show that the specific rain attenuation is not affected by the elevation angle but it is affected by the signal polarization. Accordingly, the specific rain attenuation for the horizontal polarized signal is higher for all the elevation angles than that of the vertical polarized signal. The results of the computation for the rain attenuation as a function of elevation angle are presented in Table 5 and Figure 5. The results in Table 5 and Figure 5 show that the rain attenuation is affected by the elevation angle and the signal polarization. Accordingly, the rain attenuation for the horizontal polarized signal is higher for all the elevation angles than that of the vertical polarized signal. The results in Table 5 and Figure 5 show that the rain attenuation is inversely proportional to elevation angle. Hence, the rain attenuation is high for low elevation angle but low for high elevation angle.

The results of the computation for the rain attenuation as a function of elevation angle for different rain fall exceeded percentages, P are presented in Table 6 and Figure 6. The results in Table 6 and Figure 6 show that the rain attenuation is inversely proportional to P. Hence, the rain attenuation is high for low P but low for high P.

Elevation Angle (θ°)	Rain slant path length , Ls in km	(Lg ) Horizontal projection distance of ${\rm L}_{\rm s}$ on the ground in km	Rain path length reduction factor, rp	Effective rain path length , Le in km
10	27.3	26.9	0.5	12.4
18	15.4	14.6	0.6	9.3
26	10.8	9.7	0.7	7.6
41	7.2	5.5	0.8	5.8
52	6.0	3.7	0.9	5.2
60	5.5	2.7	0.9	4.9
69	5.1	1.8	0.9	4.7
74	4.9	1.4	0.9	4.7

Table 3 The results of the computation for the rain slant path length and the effective rain path length



Figure 3 The effective rain path length versus elevation angle

Table 4 The results of the computation for the specific rain attenuation as a function of elevation angle

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Elevation Angle (θ°)	Specific Rain Attenuation in dB for horizontal polarization	Specific Rain Attenuation in dB for vertical polarization		
10	0.00981	0.00670		
18	0.00981	0.00670		
26	0.00981	0.00670		
41	0.00981	0.00670		
52	0.00981	0.00670		
60	0.00981	0.00670		
69	0.00981	0.00670		
74	0.00981	0.00670		





Elevation Angle (θ°)	Rain Attenuation in dB for horizontal polarization	Rain Attenuation in dB for vertical polarization		
10	0.122106	0.083403		
18	0.091372	0.06241 0.050648		
26	0.074151			
41	0.057113	0.03901		
52	0.050726	0.034648		
60	0.047926	0.032735		
69	0.046136	0.031513		
74	0.045673	0.031196		

Table 5 The results of the computation for the rain attenuation as a function of elevation angle



Figure 5 The graph plot for the rain attenuation versus elevation angle

Table 6 The results of the computation for the rain attenuation as a function of elevation angle for different rain fall exceeded percentages, P

Elevatio n Angle (θ°)	Rain Attenuatio n (horizontal) in dB for p = 0.001%	Rain Attenuatio n (vertical) in dB for p = 0.001%	Rain Attenuatio n (horizontal) in dB for p = 0.01%	Rain Attenuatio n (vertical) in dB for p = 0.01%	Rain Attenuatio n (horizontal ) in dB for p = 0.1%	Rain Attenuatio n (vertical) in dB for p = 0.1%	Rain Attenuatio n (horizontal ) in dB for p = 1%	Rain Attenuatio n (vertical) in dB for p = 1%
10	0.1761	0.1203	0.1221	0.0834	0.0444	0.0304	0.0085	0.0058
18	0.1318	0.0900	0.0914	0.0624	0.0333	0.0227	0.0064	0.0044
26	0.1070	0.0731	0.0742	0.0506	0.0270	0.0184	0.0052	0.0035
41	0.0824	0.0563	0.0571	0.0390	0.0208	0.0142	0.0040	0.0027
52	0.0732	0.0500	0.0507	0.0346	0.0185	0.0126	0.0036	0.0024
60	0.0691	0.0472	0.0479	0.0327	0.0174	0.0119	0.0034	0.0023
69	0.0665	0.0455	0.0461	0.0315	0.0168	0.0115	0.0032	0.0022
74	0.0659	0.0450	0.0457	0.0312	0.0166	0.0114	0.0032	0.0022



Figure 6 The results of the computation for the rain attenuation as a function of elevation angle for different rain fall exceeded percentages, P

# 4. Conclusion

Rain attenuation for a LEO satellite for different elevation angles and for different rain fall exceeded percentages, P is The studied. model used is the International power-law Telecommunication Union (ITU) rain attenuation computation model which expresses rain attenuation in terms of specific rain attenuation and some frequency and polarization dependents parameters, along with effective rain path length. The study also considered the effect of the elevation angle on the effective rain path length, the specific rain attenuation and the rain attenuation. In all, the results showed that the horizontally polarized signal had higher rain attenuation in all the elevation angles than the vertically polarized signal.

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