

Design Of Satellite Orbital Two Line Element To Cartesian Position Vector Coordinates Transformation Program

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Abstract— In this program, the design of satellite orbital Two Line Element (TLE) to Cartesian Position Vector (CVC) coordinates (X,Y,Z) transformation program is presented. The TLE dataset consists of eccentricity which is denoted as e ; inclination angle with unit in degrees and denoted i , right ascension of the ascending node with unit in degrees and denoted Ω , mean anomaly with unit in degrees and denoted as M , argument of the perigee with unit in degrees and denoted as ω , mean motion with unit in revolutions per day and denoted as n , and revolution number at epoch and denoted as N_{ap} . The program designed consisted of three modules and the detailed algorithm for each of the modules is presented. Five cases study satellites were used in the study and the output data includes the orbital period, the semi major axis, the semi minor axis, the eccentric anomaly, and the Cartesian coordinates X, Y, and Z for the five case study satellites. The results for the five satellites were presented in tables and graphs. The results showed that for the five satellites, the correlation between E and M is 0.984041669 whereas the correlation between E and e is 0.563807015. In essence E is more correlated to M than it is to e . In all, the results showed that the absolute value of X,Y,Z coordinates can be as high as the semi major axis of the satellite's orbit.

Keywords — Coordinates Transformation, Two Line Element , Orbital Coordinates, Satellite, Cartesian Position Vector Coordinates

1. Introduction

Satellites position in orbits are in different ways or formats known as coordinate systems [1,2,3,4,5,6,7,8,9,10,11,12,13]. Each of the coordinate systems presents the location of the satellite in a way that is useful for some specific applications or they make it easier or better to visualize and apply the coordinates in specific analysis and processes. One of the most popular ways of

representing satellites orbital parameters is the Two Line Element (TLE) format [14,15, 16,17, 18,19, 20,21,22,23]. The TLE is used to capture and store historical data about the positions of the satellite at any given instance of time, referred to as epoch. However, the TLE format is not suitable for certain applications of the satellites data [24,25, 26,27, 28,29, 30,31, 32]. As such, coordinate transformation is needed [33,34, 35,36, 37,38, 39].

Accordingly, a program is designed in this paper for the transformation of satellites TLE datasets to their corresponding Cartesian position vector coordinates [40,41,42,43,44,45,46]. The program algorithms are presented along with the numerical computation results obtained from the program for a selected number of case study satellites. The program is implemented using the Visual Basic for Application [47,48,49,50,51,52].

2. Methodology

The program design presented in this paper can read in a satellite's Two Line Element (TLE) dataset and then compute the equivalent Cartesian Position Vector (CPV) format transformation of the TLE dataset.

The TLE dataset consists of eccentricity which is denoted as e ; inclination angle with unit in degrees and denoted i , right ascension of the ascending node with unit in degrees and denoted Ω , mean anomaly with unit in degrees and denoted as M , argument of the perigee with unit in degrees and denoted as ω , mean motion with unit in revolutions per day and denoted as n , and revolution number at epoch and denoted as N_{ap} .

The satellite Cartesian coordinates, x , y and z are computed from the listed TLE dataset , namely, e , i , Ω , M , ω , n , and N_{ap} . However, some other orbital parameters of the satellite that are required for the computation of the Cartesian coordinates, x , y and z are determined from the given TLE dataset. Such additional orbital parameters include; the

orbital period with unit as days and denoted as T, the semi major axis, with unit as km and denoted as a, the semi minor axis with unit as km and denoted b and the eccentricity anomaly with unit in degrees is denoted E. This set of additional orbital parameters are denoted in this paper as secondary orbital elements, namely, T, a, b, and E. The computation of T, a and b are based on simple closed-form analytical expressions. However, the computation of E from the values of M and e is performed using iterative procedure presented by [53]. The analytical expressions for the computation of the satellite Cartesian coordinates, x, y and z are given as follows;

$$T = \frac{1}{n} \tag{1}$$

$$GM = 2.9755364 \times 10^{15} \text{ km}^3 / \text{day}^2.$$

$$a = \sqrt[3]{\left(\frac{GM}{4\pi^2}\right) T^2} \tag{2}$$

$$b = \sqrt[2]{a^2(1 - e^2)} \tag{3}$$

$$E = M + e(\sin(E)) \tag{4}$$

E is determined using iterative method based on the algorithm presented by [53];

$$x3 = (a) \cos(E) - (a)e \tag{5}$$

$$y3 = (b) \sin(E) \tag{6}$$

$$z3 = 0 \tag{7}$$

$$x2 = (x3) \cos(\omega) - (y3) \sin(\omega) \tag{8}$$

$$y2 = (x3) \sin(\omega) + (y3) \cos(\omega) \tag{9}$$

$$z2 = z3 \tag{10}$$

$$x1 = x2 \tag{11}$$

$$y1 = (y2) \cos(i) - (z2) \sin(i) \tag{12}$$

$$z1 = (y2) \sin(i) + (z2) \cos(i) \tag{13}$$

$$x = (x1) \cos(\Omega) - (y1) \sin(\Omega) \tag{14}$$

$$y = (x1) \sin(\Omega) + (y1) \cos(\Omega) \tag{15}$$

$$z = z1 \tag{16}$$

The three modules designed for the computation of the satellite Cartesian coordinates, x,y and z from the TLE dataset are as follows;

- i. Algorithm 1 Module1 Input TLE_Compute_XYZ()
- ii. Algorithm 2 Module 2 Compute_E(M, e)
- iii. Algorithm 3 Module 3 Compute_XYZ (e, i, Ω, M, ω, n, N_{ap}, T, a, b, E, x, y, z)

The detail algorithm for each of the three modules are presented next.

i). Algorithm 1 Module1 Input TLE_Compute_XYZ()

Algorithm 1 The procedure for Module1 Input TLE_Compute_XYZ()

```

1:Inpute Satellite_name, e, i, Ω, M, ω, n, Nap
2: T = 1/n
3: GM = 2.9755364x1015
4:a =  $\sqrt[3]{\left(\frac{GM}{4\pi^2}\right) T^2}$ 
5:b =  $\sqrt[2]{a^2(1 - e^2)}$ 
6: E =Module_Compute E(M,e) // call module compute E(M,e) and assign the returned value from the module to E
7: Call Module 3 ComputeXYZ (e, i, Ω, M, ω, n, Nap, T, a, b, E, x, y, z)
8: Return E(k)
10: End Module compute E()

```

ii). Algorithm 2 Module 2 Compute_E(M, e).

E is determined using iterative method based on the algorithm presented by [53] and it is presented as follows;

Algorithm 2 The procedure for Module 2 Compute_E(M, e)

```

1: Input er
2: k =0;
3: E(k) = M
4: fE(k) = E(k) - M - e*Sin(E(k))
5: dfE(k) = 1 - e*Cos(E(k))
6: k = k+1
7: E(k) = E(k-1) -  $\frac{E(k-1)-M - e*Sin(E(k-1))}{1 - e*Cos(E(k-1))}$ 
8: if ( |E(k) - E(k - 1)| > |er|) then Goto step 4endif
9: Return E(k)
10: End Module compute E()

```

iii). Algorithm 3 Module 3 Compute_XYZ (Satellite_name, , e, i, Ω, M, ω, n, N_{ap}, T, a, b, E, x, y, z)

Algorithm 3 The procedure for Module 3 Compute_XYZ (Satellite_name, e, i, Ω, M, ω, n, N_{ap}, T, a, b, E, x, y, z)

```

1: x3 = (a) cos(E) - (a)e
2: y3 = (b) sin(E)
3: z3 = 0
4: x2 = (x3) cos(ω) - (y3) sin(ω)
5: y2 = (x3) sin(ω) + (y3) cos(ω)
6: z2 = z3
7: x1 = x2
8: y1 = (y2) cos(i) - (z2) sin(i)

```

- 9: $z1 = (y2) \sin(i) + (z2) \cos(i)$
- 10: $x = (x1) \cos(\Omega) - (y1) \sin(\Omega)$
- 11: $y = (x1) \sin(\Omega) + (y1) \cos(\Omega)$
- 12: $z = z1$
- 13: Output Satellite name , e, i, Ω , M, ω , n, N_{ap}
- 14: Output Satellite name, T, a, b, E, x, y, z
- 15: Return
- 16: End Module compute E()

of the coordinate transformation. The five satellites, as presented in Table 1 includes RESURS-DK 1, CUBESAT XI-V and CALSPHERE 1 which are low Earth orbit (LEO) satellites, LAGEOS 1 which is a medium Earth orbit (MEO) satellite and INMARSAT 3-F1 which is a geostationary Earth orbit (GEO) satellite. All the five selected satellites are operational. The NORAD Two Line Element (TLE) dataset for the five active satellites, with data current as of 2022 Jul 02 12:05:26 UTC (Day 183) are presented in Figure 1 as accessed from [54].

3 Numerical Example

The two line element dataset for five selected satellites are used to demonstrate how the programs presents the results

Table 1 The five selected case study satellites (Source: <https://in-the-sky.org/> and <https://www.n2yo.com/>)

| S/N | NORAD ID | Satellite Name | Launch date | Status | Category | Orbital height (km) | Owner |
|-----|----------|----------------|-------------|-------------|----------------------------------|---------------------|--|
| 1 | 29228 | RESURS-DK 1 | 14 Jun 2006 | Operational | Earth Resources (LEO) | 556 | Commonwealth of Independent States (former USSR) |
| 2 | 28895 | CUBESAT XI-V | 26 Oct 2005 | Operational | Amateur radio and CubeSats (LEO) | 679 | Japan |
| 3 | 900 | CALSPHERE 1 | 05 Oct 1964 | Operational | Radar Calibration (LEO) | 985 | United States |
| 4 | 8820 | LAGEOS 1 | 03 May 1976 | Operational | Geodetic (MEO) | 5893 | United States |
| 5 | 23839 | INMARSAT 3-F1 | 02 Apr 1996 | Operational | Geostationary (GEO) | 35866 | International Mobile Satellite Organization (INMARSAT) |

```

RESURS-DK 1
1 29228U 06021A 22182.85702829 .00000388 00000-0 35839-4 0 9998
2 29228 69.9357 92.3092 0003328 355.7535 4.3598 15.03268924884546

CUBESAT XI-V
1 28895U 05043F 22182.79982544 .00000335 00000-0 72377-4 0 9998
2 28895 98.1087 313.9583 0018036 96.4060 263.9198 14.64366421889518

CALSPHERE 1
1 00900U 64063C 22183.60674226 .00000326 00000-0 33757-3 0 9996
2 00900 90.1742 41.1916 0026876 341.5197 71.8743 13.73830012872741

LAGEOS 1
1 08820U 76039A 22182.72361315 .00000013 00000-0 00000-0 0 9990
2 08820 109.8554 43.8842 0045063 251.7017 295.8809 6.38664942820764

INMARSAT 3-F1
1 23839U 96020A 22182.42771380 -.00000255 00000-0 00000-0 0 9992
2 23839 7.5677 58.0387 0009065 47.6313 261.1318 0.99987079 95783
    
```

Figure 1 The NORAD Two Line Element (TLE) dataset for the five active satellites, with data current as of 2022 Jul 02 12:05:26 UTC (Day 183) accessed from [54].

4. Results and Discussions

The detailed TLE dataset were extracted from the NORAD Two Line Element (TLE) dataset for the five active satellites presented in Figure 1 and the extracted TLE parameters are shown in Table 2. The datasets in Table 2 are then used to compute the orbital period, semi major axis, semi minor axis and the eccentric anomaly, as well as the Cartesian coordinates X, Y, and Z for the five case study satellites and the results are shown in Table 3. Furthermore, the graph of the eccentricity anomaly E versus

mean anomaly (M) and the eccentricity anomaly (E) versus eccentricity (e) were plotted as shown in Figure 2 and Figure 3 respectively. It was also determined that for the five satellites, the correlation between E and M is 0.984041669 whereas the correlation between E and e is 0.563807015. In essence E is more correlated to M. The bar chart of the Cartesian coordinates X, Y, and Z for the five case study satellites is given in Figure 4.

Table 2 The detail TLE dataset extracted for Figure 1 for the five selected satellites

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|----------------|-----------|---------|----------------|---------|----------------|-------------|-------|
| Satellite Name | e | i (deg) | Ω (deg) | M (deg) | ω (deg) | n (rev/day) | Nap |
| RESURS-DK 1 | 0.0003328 | 69.9357 | 92.3092 | 4.3598 | 355.754 | 15.03269 | 88454 |
| CUBESAT XI-V | 0.0018036 | 98.1087 | 313.958 | 263.92 | 96.406 | 14.64366 | 88951 |
| CALSPHERE 1 | 0.0026876 | 90.1742 | 41.1916 | 71.8743 | 341.52 | 13.7383 | 87274 |
| LAGEOS 1 | 0.0045063 | 109.855 | 43.8842 | 295.881 | 251.702 | 6.386649 | 82076 |
| INMARSAT 3-F1 | 0.0009065 | 7.5677 | 58.0387 | 261.132 | 47.6313 | 0.999871 | 9578 |

Table 3 The results of the computation of the orbital period, semi major axis, semi minor axis, the eccentric anomaly, the Cartesian coordinates X, Y, and Z for the five case study satellites

| | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
|----------------|-----------|-----------|-----------|---------|-----------|------------|-----------|
| Satellite Name | T (day) | a (km) | b (km) | E (deg) | X | Y | Z |
| RESURS-DK 1 | 0.0665217 | 6,934.96 | 6,934.96 | 4.36 | -284.15 | 6,926.82 | 13.21 |
| CUBESAT XI-V | 0.0682889 | 7,057.25 | 7,057.24 | 263.82 | 4,898.12 | -5,082.55 | 14.68 |
| CALSPHERE 1 | 0.0727892 | 7,363.99 | 7,363.96 | 72.02 | 3,290.80 | 2,856.07 | 5,928.91 |
| LAGEOS 1 | 0.1565766 | 12,271.18 | 12,271.06 | 295.65 | -9,116.36 | -8,052.97 | -1,427.15 |
| INMARSAT 3-F1 | 1.0001292 | 42,244.73 | 42,244.72 | 207.75 | 28,744.81 | -30,531.89 | -5,387.16 |

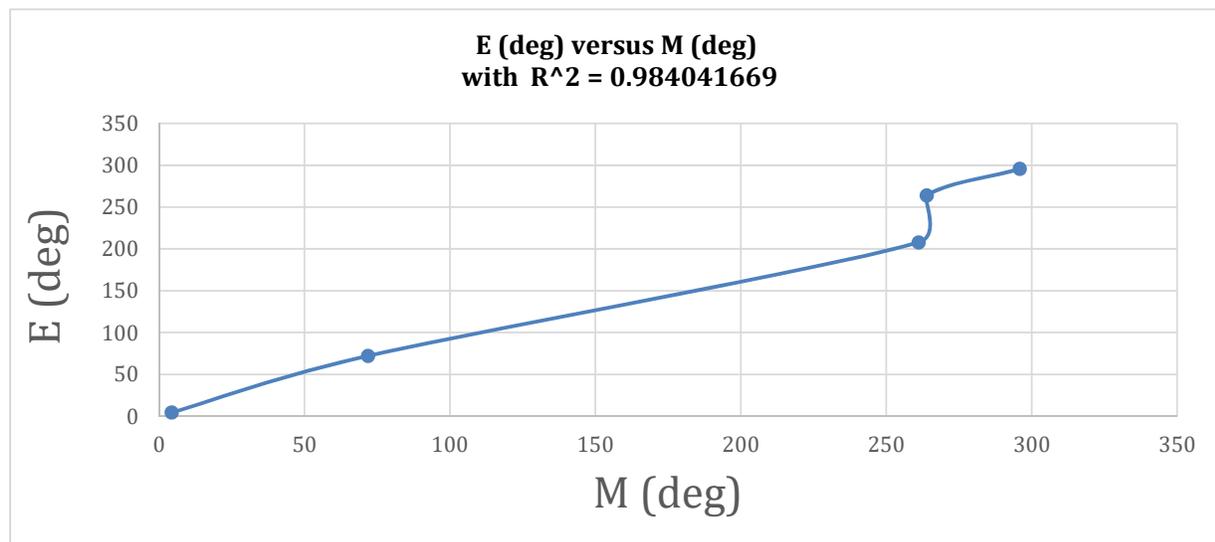


Figure 2 The graph of the eccentricity anomaly, E versus mean anomaly (M) for the five case study satellites

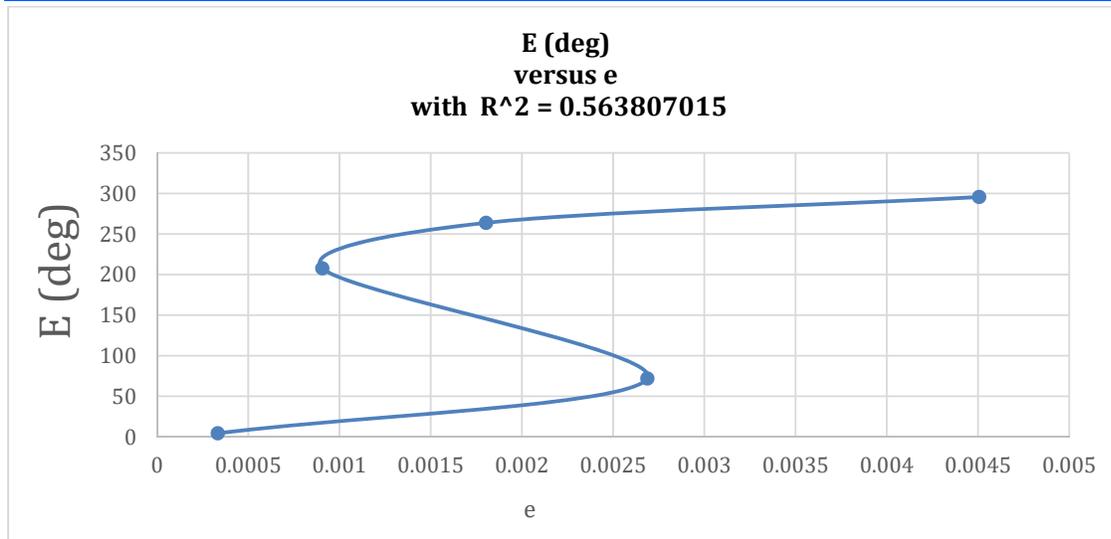


Figure 3 The graph of the eccentricity anomaly, E versus eccentricity (e) for the five case study satellites

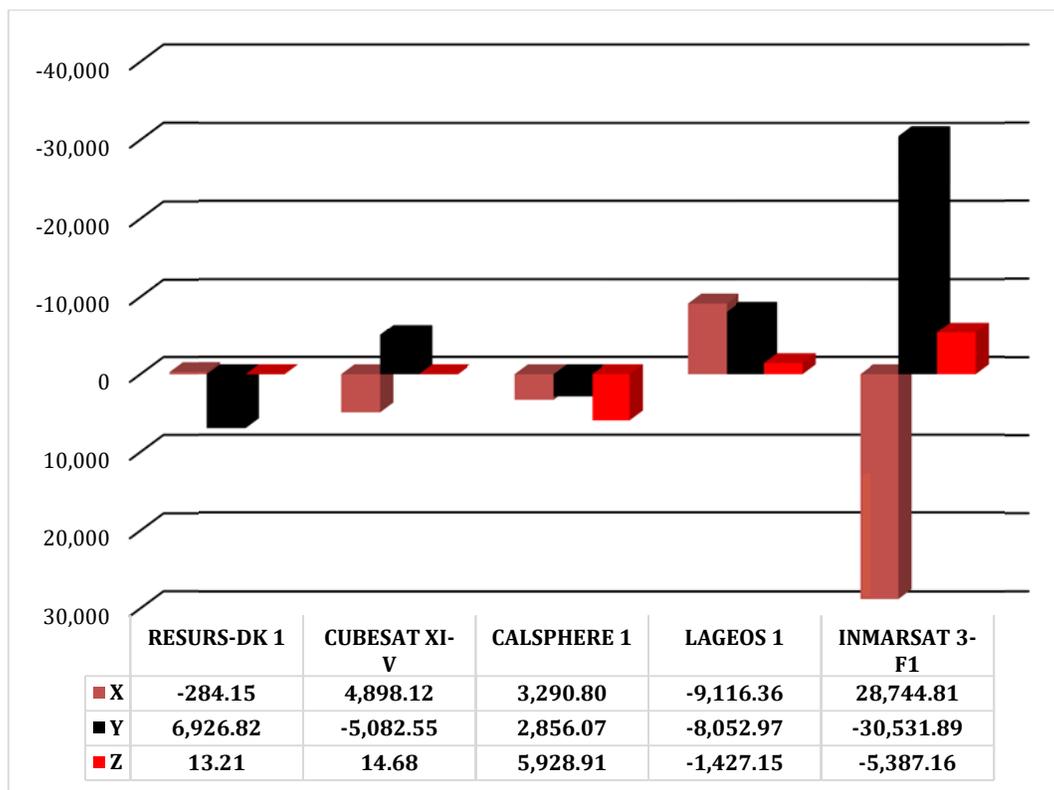


Figure 4 The bar chart of the Cartesian coordinates X, Y, and Z for the five case study satellites

5. Conclusion

The design of the modules and their corresponding algorithms for computing the Cartesian coordinates X, Y, and Z of a satellite from the two line element dataset are presented. The design consists of three modules and five case study satellites are used to show how the program modules are applied in the computation. In the numerical examples, the output data includes the orbital period, the semi major axis, the semi minor axis, the eccentric

anomaly, and the Cartesian coordinates X, Y, and Z for the five case study satellites

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